

# Ruckus League

**Input File:** *ruckusin.txt*

**Output File:** *ruckusout.txt*

It's that time of year again! The Annual Ruckus World Championships is fast approaching and you are absolutely determined to see Australia victorious. As the name implies, the goal of the competition is to be as loud and obnoxious as possible. Players compete in teams of at least  $M$  people (there is no upper limit on team sizes). To make sure teams don't mix, team members must hold hands with each other.

Of course, you've found that there is nothing *more obnoxious* than spoilt kindergarteners, so you've rounded up  $N$  of the loudest ones you could find. You were hoping to send as many teams as possible, but some of the children have already started holding hands with their friends<sup>1</sup>. Being as stubborn as they are, you are finding it rather difficult to convince them to let go of each other, or even to hold hands with anyone else.

Now for any other person, the story would end here; you'd have to send whatever teams their 'friendships' have forged. However, being the social engineering master you are, you've brought  $K$  lollipops to use to bribe the children. You can pass a lollipop to the hand of a child, which will make them let go of the hand they are holding<sup>2</sup>.

Using your  $K$  lollipops, what is the largest number of teams with at least  $M$  children you can form?

## Input

The first line of the input file will contain four space separated integers on a single line, in the format: " $N L K M$ ".

- $N$  is the number of children you have gathered.
- $L$  is the number of pairs of hands that are already joined together.
- $K$  is the number of lollipops you have.
- $M$  is the minimum size of a team. All teams must have at least  $M$  people.

The following  $L$  lines will each contain two integers, in the format: " $l_i r_i$ ". This indicates that the  $l_i$ th child's left hand is holding the  $r_i$ th child's right hand. The children are numbered from 1 to  $N$ . No one can hold their own hands.

## Output

Output should consist of a single integer: the maximum number of teams with at least  $M$  children you can form.

(continued over ...)

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<sup>1</sup>Everyone has exactly two hands, each of which can hold up to one other hand. They learnt all this (and more) in kindergarten.

<sup>2</sup>It's as easy as *giving* candy to a baby.

**Sample Input 1**

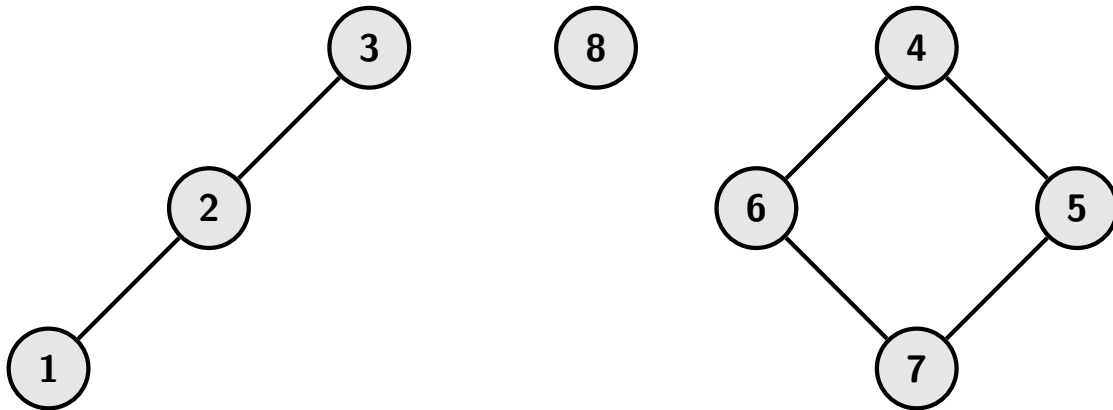
```
8 6 0 1
1 2
4 6
5 4
2 3
7 5
6 7
```

**Sample Output 1**

3

**Explanation**

In the first example, you cannot break up any pair of hands (since you have no lollipops), and teams can have any number of people in them. Initially, the children have formed three teams: one of size 3, one of size 4 and one of size 1. Thus the output should be 3.



*(continued over ...)*

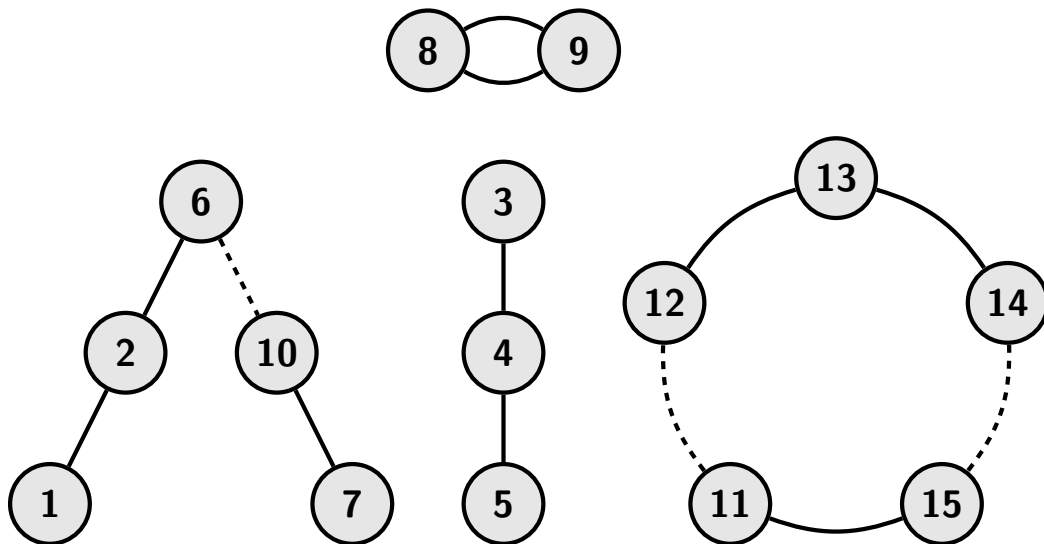
**Sample Input 2**

```

15 13 5 2
1 2
2 6
6 10
10 7
8 9
9 8
3 4
4 5
15 11
11 12
12 13
13 14
14 15
    
```

**Sample Output 2**

6



**Explanation**

In the second example, each team needs at least 2 people. Currently there are four teams of size 2, 3, 5 and 5. (The team of size 2 consists of children 8 and 9 holding *both* hands with each other.) By breaking the friendships 6 – 10, 14 – 15, 11 – 12, we can create up to six teams, of size 2, 2, 2, 3, 3 and 3. Thus the best answer is 6.

Note that even though we have 5 lollipops, we don't have to use them all in order to make the maximum number of teams (even though we can).

(continued over ...)

## Subtasks & Constraints

For all subtasks,  $0 \leq L \leq N$ ,  $1 \leq M \leq N$  and  $0 \leq K \leq L$ .

- For Subtask 1 (20 marks),  $K = 0$ ,  $M = 1$  and  $N \leq 1\,000$ .
- For Subtask 2 (20 marks),  $K = 0$  and  $N \leq 100\,000$ .
- For Subtask 3 (20 marks),  $N \leq 100\,000$  and everybody is holding hands with exactly two other people.
- For Subtask 4 (20 marks),  $N \leq 100\,000$ . Additionally, if the  $i^{\text{th}}$  person is holding hands with two people, then they are holding hands with one person with a number less than them and one with a number greater. If they are holding hands with one or no person, this condition does not apply.
- For Subtask 5 (20 marks),  $N \leq 100\,000$  and no further constraints apply.

## Scoring

The score for each input scenario will be 100% if the correct answer is written to the output file, and 0% otherwise.